## Classical Test Theory

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#### Reliability

- Reliability = stability: a measure is said to be reliable if it has the same results if the object did not change.
- Disregard uniform (systematic) bias: reliability = correlation between two measurements.
- Reliability refers to <u>random</u> measurement error:
  - EXP(error) = zero
  - No correlaton of errors with true score or any other score.

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#### True scores & reliability designs Observed score = true score + random error. We can estimate reliability by using the measure (at least) twice.

- Parallel: Simply repeat the same questions.
- Test-retest: repeat the questions with some interval (that is long enough to forget the errors in the previous respons).
- Alternative forms: ask the questions is a different format that will make respondents forget their errors instantaneously.
  Split-half: test-retest using two halves of the indicators.
- Split-half: test-retest using two halves of the indicators.
- Internal consistency: parallel measures using all possible halves of the indicators.

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### Common Factor Analysis

- Common Factor Analysis (SPSS: Principal Axis Factoring = PAF) can estimate this model from data.
- Let's look at some simple simulations.
- Note that the model does not use a reliability coefficient it builds it into the model.

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### Principal Component Analysis

- PCA is the default option in SPSS Factor, but in fact it is not (common) factor analysis at all.
- PCA: how can I create a sum-score from a set of indicators that has maximal variance.
- VAR(a+b)=VAR(a)+VAR(b)+2\*COVAR(a,b).
- PCA: largest weights for variables with strong correlations.
- While PCA and PAF ask very different questions, the answers are likely to be very similar.

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PAF and PCA

- PCA leads directly to component scores, PAF leads to estimated correlations in a latent variables model.
- PCA is computationally stable, PAF may run into problems if the model does not apply.
- PAF fits out common sense measurement models very well, PCA is harder to understand. In particular (oblique) rotation is hard to interpret in PCA, but easy to understand in PAF.

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# PAF, PCA and Cronbach's alpha

- Cronbach alpha takes a middling ground between PAF and PCA.
  - PCA: Cronbach's alpha is optimal when variation of the sum-score is maximal.
  - PAF: alpha estimates reliability when all indicators are equally correlated (= have same amount of random error). Loading =  $\sqrt{\alpha}$ .

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- Not all error can be assumed to be random!
- Systematic error = correlated error = when error arise in similar indicators in the same way!
- Latent variable models (but not in SPSS) can estimate (and control) this type of error, provided the error is repeated!
- MTMM: multiple measures of multiple constructs (traits).

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## LISREL

- LISREL = Linear Structural Relations
- Karl Jöreskog & Dag Sörbom
- Related programs: AMOS, EQS, Mplus
- Lisrel is little else but a computer program to solve an (overdetermined) set of linear equations.

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